

# Government Reference Link Models: **ORCA**

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# Mathematical Link Models

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- Government will provide mathematical models for
  - Uplink (slant) paths
  - Downlink (slant) paths
  - Horizontal paths
- Models can be useful tool for system design

# References

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L. C. Andrews and R. L. Phillips, *Laser Beam Propagation Through Random Media*, 2<sup>nd</sup> ed., SPIE Press (2005).

L. C. Andrews, R. L. Phillips, and C. Y. Hopen, *Laser Beam Scintillation with Applications*, SPIE Press (2001).

L. C. Andrews, *A Field Guide to Atmospheric Optics*, SPIE Press (2004).

# Optical Atmospheric Propagation Effects

- **Absorption & Scattering (extinction)**

- Attenuation of optical wave
- Reduces received power
- Limits optical channel availability in the presence of fog or clouds

- **Fluctuations in Index of Refraction**

- Small temperature fluctuations cause refractive-index fluctuations known as *optical turbulence*
- Cause intensity and phase fluctuations on propagating beam

- **Atmospheric Links**

- Extended path – turbulence between Transmitter and Receiver (Tx & Rx)
  - Uplink/downlink to/from aircraft
  - Aircraft to aircraft
- Aero-optic effect around aircraft, especially with external dome
  - Modeled as thin turbulent layer (phase screen) near Tx/Rx

- *Propagation Effects on Beam*

- Larger beam spot size at receiver
  - Leads to additional power loss in signal
- Beam wander
  - Caused by turbulent eddies near Tx
  - Contributes to long-term spot size
  - Can contribute to scintillation
- Scintillation (intensity fluctuations)
  - Reduces signal-to-noise ratio (SNR)
  - Leads to signal fades
- Phase fluctuations
  - Angle-of-arrival fluctuations (causes beam jitter on detector)
  - Reduces spatial coherence of beam (determines speckle size at Rx)
  - Limits heterodyne efficiency in coherent detection
  - Limits "effective" Rx aperture size for improved SNR to size of  $r_0$

$r_0$  = Fried's parameter

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- **Atmospheric Links**

- Extended path turbulence between Transmitter and Receiver (Tx & Rx)
  - Uplink/downlink to/from air
  - Aircraft to aircraft
- Aero-optic effect around aircraft, especially with external dome
  - Modeled as thin turbulent layer (phase screen) near Tx/Rx

- **Propagation Effects on Beam**

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# Mitigation of Atmospheric Effects on Optical Communication Link

## • **Transmitter System Architecture**

- *Increase transmitted power*
  - Improve SNR at Rx
- *Multiple beams*
  - Sufficiently separated to ensure statistical independence at Rx
  - Produces aperture averaging of scintillation (similar to receiver array)
- *Multi-mode beams*
- *Partially coherent beams*
- *Multiple frequency regimes*
  - RF and optical
- *Adaptive optics*
  - Corrects phase distortions caused by optical turbulence

## • *Receiver System Architecture*

- *Incoherent (direct) detection*
  - intensity modulation
  - large aperture receiver (improve reliability)
  - array receivers (improve reliability)
- *Coherent (heterodyne) detection*
  - intensity and phase modulation
  - large aperture receiver
  - array receivers

# Mitigation of Atmospheric Effects on Optical Communication Link

- **Transmitter System Architecture**

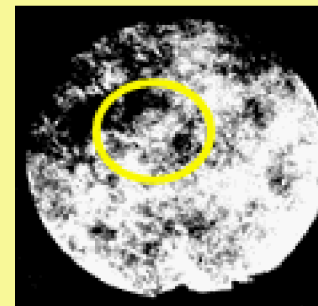
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- **Receiver System Architecture**

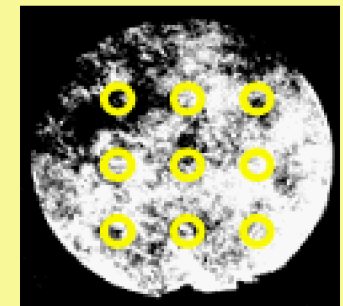
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  - large aperture receiver
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Intensity cross-section of beam after propagating thru extended turbulence. Dark patches denote a signal fade and yellow circle(s) depict (a) a large Rx aperture or (b) an array of small Rx apertures.

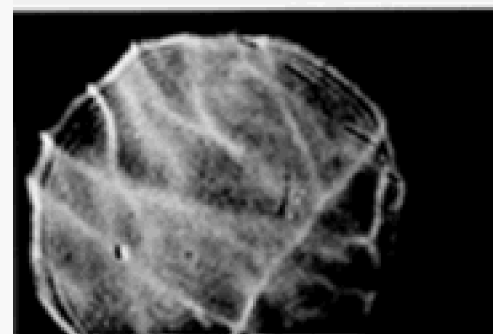
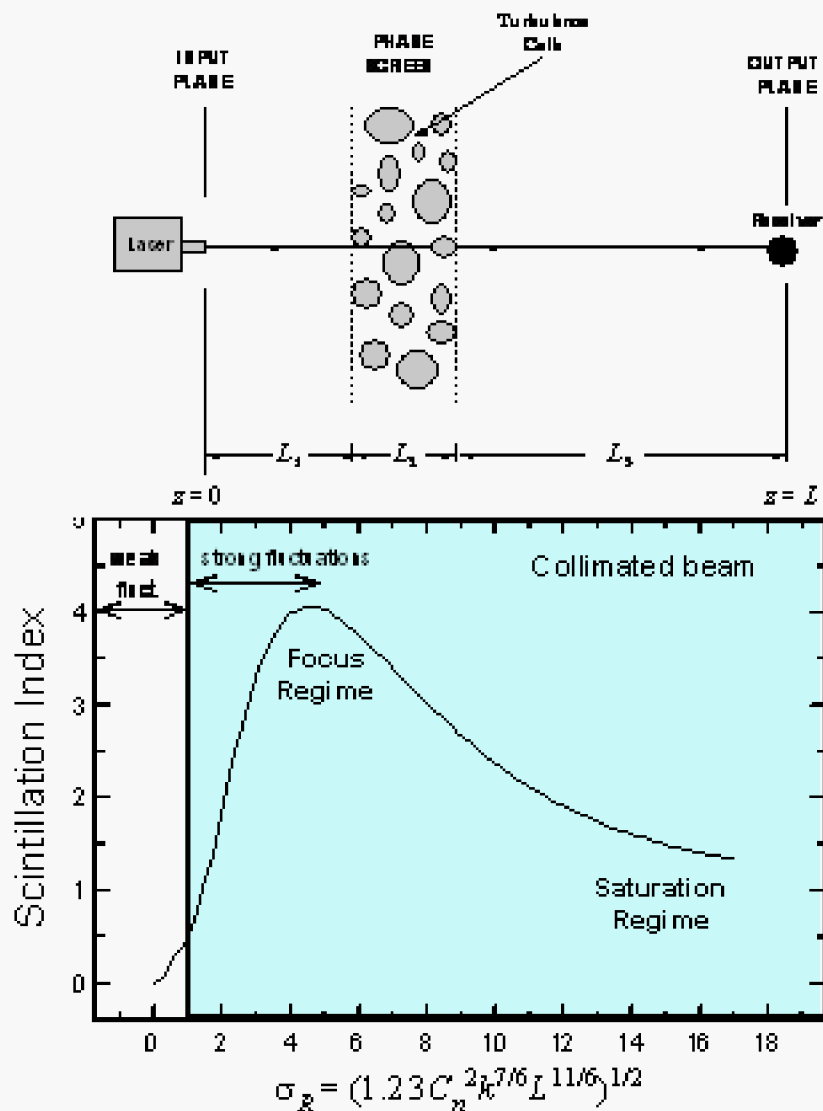
(a)



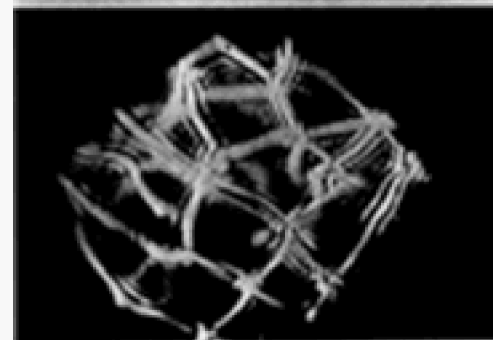
(b)



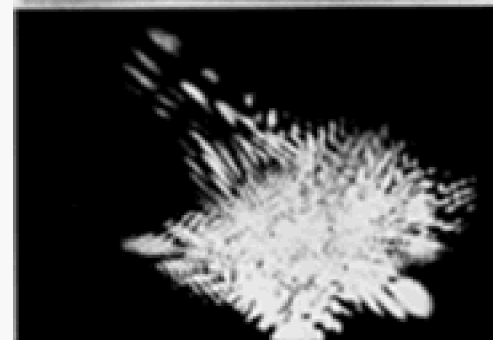
# Intensity Fluctuations



**Emerging From  
Phase Screen**



**Focusing  
Regime**



**Saturation  
Regime**

**Figure** Intensity profile of beam after passing through phase screen, immediately beyond (bottom), further beyond (middle), and far beyond (top) .



# Mathematical Formulas

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## Propagation Paths

- *Uplink* (slant) path from ground to aircraft
- *Downlink* (slant) path from aircraft to ground
- *Horizontal* path between two aircraft

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# Atmospheric Models

Kolmogorov Spectrum:

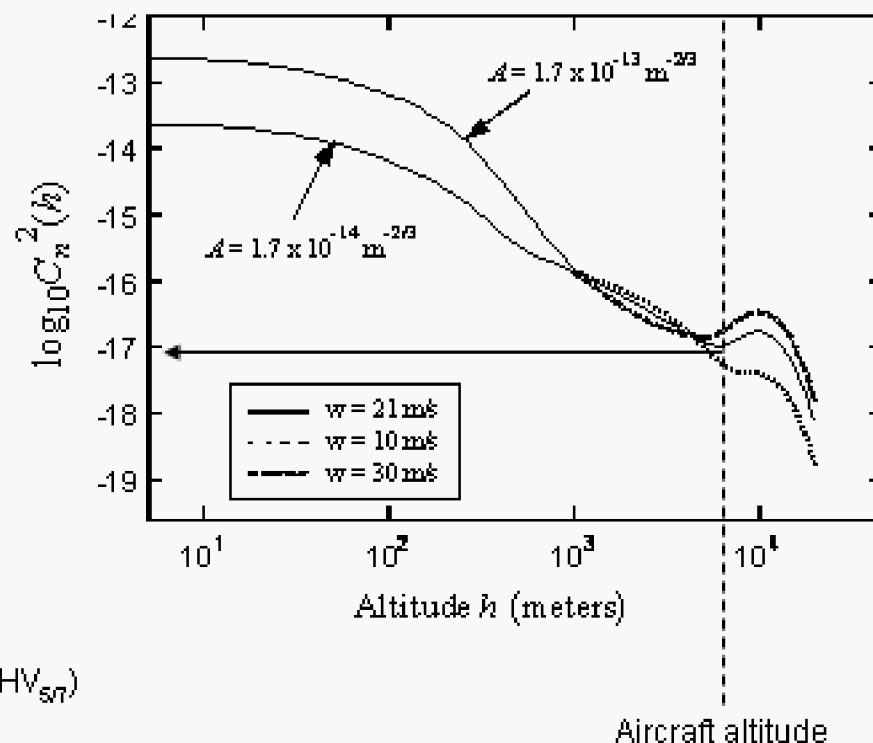
$$\Phi_n(\kappa, h) = 0.033 C_n^2(h) \kappa^{-11/3}$$

Hufnagle-Valley (HV):

$$\left\{ \begin{aligned} C_n^2(h) = & 0.00594 \left( \frac{w}{27} \right)^3 (10^{-3} h)^{10} \exp\left(-\frac{h}{1000}\right) \\ & + 2.7 \times 10^{-11} \exp\left(-\frac{h}{1500}\right) + A \exp\left(-\frac{h}{100}\right) \end{aligned} \right.$$

where

- $h$  = altitude
- $w$  = upper atmospheric pseudo-wind speed (= 21 m/s for HV<sub>SN</sub>)
- $A = C_n^2$  near ground level (=  $1.7 \times 10^{-14} \text{ m}^{-2/3}$  for HV<sub>SN</sub>)



# CONCLUDING REMARKS

- **Scintillation index** (variance/mean<sup>2</sup>) may be worse at weaker  $C_n^2$
- **Aperture averaging** can reduce signal fluctuations
- **Speckle size** at long ranges through weak  $C_n^2$  values may be too large for single aperture averaging
- **Array of small receivers** (properly separated) can reduce scintillation index more than single large aperture
- **Multiple beams** can reduce scintillation like an array of receivers

